

H₂ Phase Transition + Gravity = Substellar H₂ Bodies

Introduction

- Observations of various ices and of comets
→ Phase transition processes are happening in cold regions
- Fragmentation of gravitationally unstable fluids in a phase transition
→ Formation of cold, substellar sized bodies^[1,2]

H₂ condensation conditions

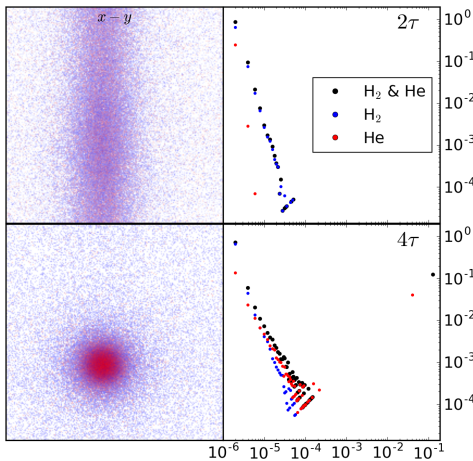
- During the plane-parallel contraction of star formation
- Dense substellar structures such as cometary knots

Motivation

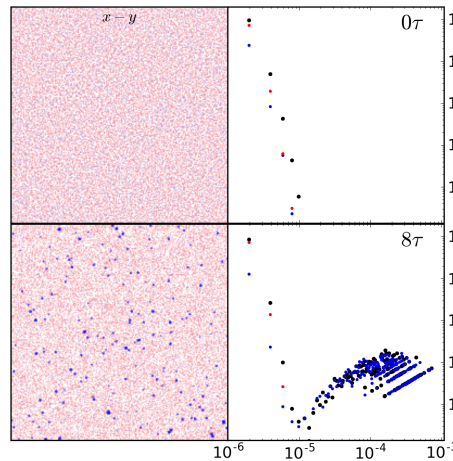
- Formation of solid H₂ during star formation
- Solid H₂ as dark baryons
- Formation of solid H₂ in clumpuscules
- Formation of solid H₂ in cometary knots
- Comets as remnants of solid H₂

Conclusions

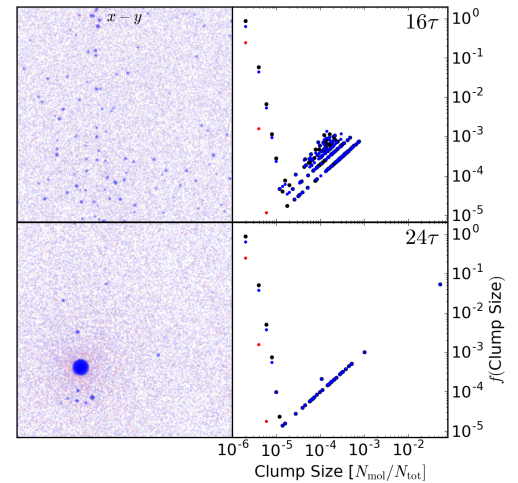
- Fluids in a phase transition are always gravitationally unstable
→ Jeans length vanishes
- H₂ phase transition + gravity:
Gas $\xrightarrow[\text{transition}]{\text{phase}}$ grains $\xrightarrow[\text{transition}]{\text{gravity}}$ comets / planetoids
- Sheet-like collapse
→ Fastest collapsing geometry
→ Temperature increase by only a factor of 2
→ Smallest opacity increase
- H₂ phase transition can be reached during sheet-like collapse, if
 $T_0 < 15$ K without cooling
 $T_0 < 30$ K with cooling
- H₂ condensation
→ Inefficient star formation
→ Difficult to detect, dark baryons?



Ideal gas with 75% H₂ + gravity ($L > \lambda_{\text{Jeans}}$)
→ Formation of gaseous He-planetoid



Phase transition with 25% H₂, without gravity
→ Formation of solid H₂-oligomers



Phase transition with 75% H₂ + gravity ($L < \lambda_{\text{Jeans}}$)
→ Formation of solid H₂-planetoid

Physics

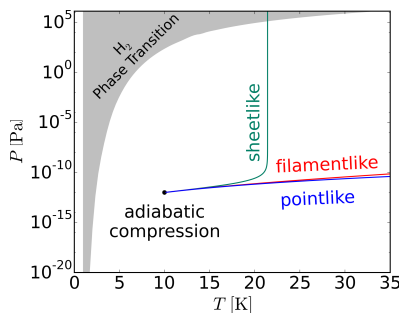
- Phase transition fluid: $(\partial P / \partial \rho)_s = 0$
 - Increase of density does not increase pressure
 - Increase of density increases fraction of condensed matter
- Fluids in a phase transition are gravitationally unstable at any scale
- Virial theorem using the inter-molecular Lennard-Jones potential energy $E_{LJ} = E_a + E_r$ and gravitational potential E_G :

$$0 = \underbrace{2E_{\text{kin}} + 12E_r}_{>0} + \underbrace{6E_a + E_G}_{<0}$$

- Unvirializable density domain if $6|E_a| > 2E_{\text{kin}} + 12E_r$
- Formation of H₂ clumps up to $T \approx 600$ K

Sheetlike Collapse

- Fastest collapsing geometry^[3]
- Remains optically thin
- Temperature increase by a factor of ≤ 2.1
- Phase transition if $T < T_c \equiv 33$ K
 - $T_c/2.1 \approx 15$ K
 - Phase transition if $T < 15$ K

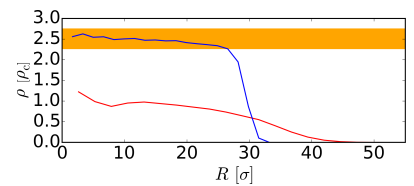


Simulations

- Widely used Molecular dynamics code: LAMMPS^[4]
- Combination of Lennard-Jones and gravitational potential
- Use of Super-Molecules:
 - 1 Super-Molecule = η molecules
 - Invariance of $E_{\text{kin}}, E_{LJ}, E_G$

Planetoid Densities

- Rocky H₂ planetoid
- Gaseous He planetoid
- Laboratory condensed H₂



References

- (1) Füglistaler A., Pfenniger D. 2015, *Astronomy & Astrophysics*, 578, A18
- (2) Füglistaler A., Pfenniger D. 2016, *Astronomy & Astrophysics*, 591, A100
- (3) Zel'dovich, Y. B. 2016, *Astronomy & Astrophysics*, 5, 84
- (4) Plimpton S. 1995, *J Comp Phys*, 117, 1-19

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